

## Project SM06

# Design with Plastics for Long-term Performance

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# Project objective

- Develop a capability to design with polymers under long-term load
  - Develop a model for deformation of polymers under a simple load history – *constant stress*
    - Include non-linear behaviour
    - Generalise to multiaxial stress states
  - Develop methodology for using creep data to predict performance under varying stress
  - Prepare code to implement the model in a finite element system
  - Evaluate code

# Summary of progress

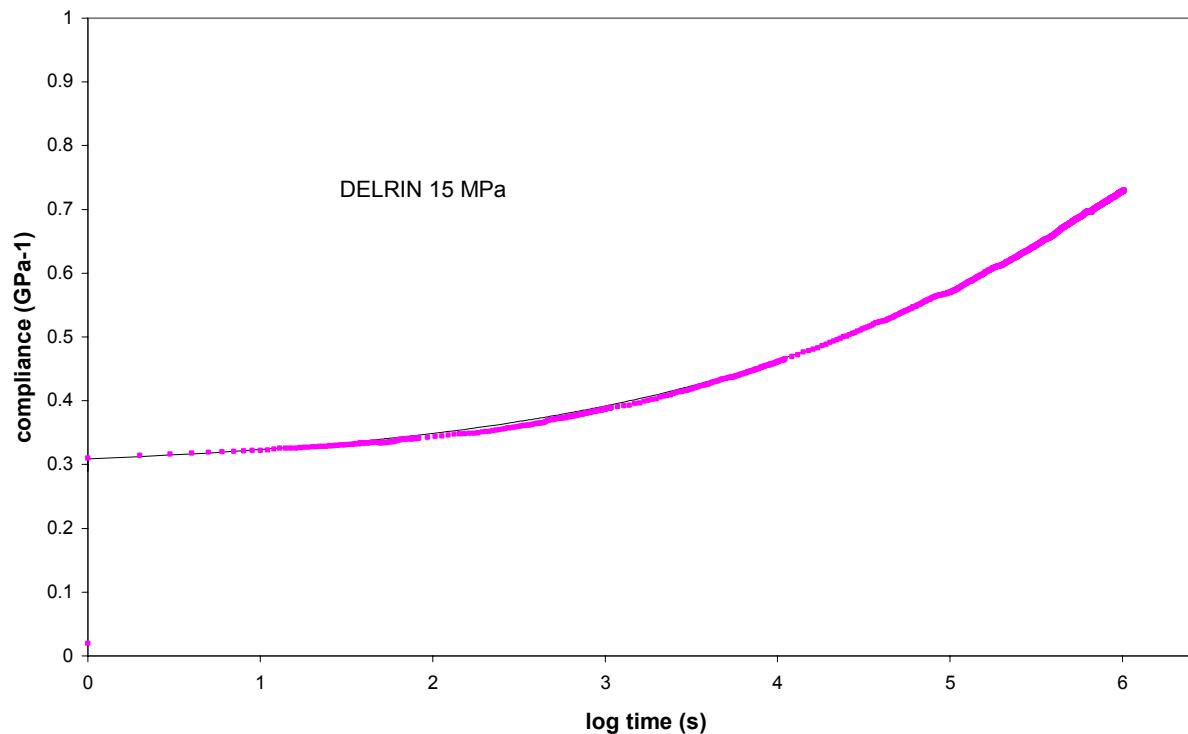
- **Materials**
  - Poly(oxymethylene) Du Pont DELRIN compression moulded
  - POM Du Pont DELRIN injection moulded – tested along flow
  - POM Ticona HOSTAFORM injection moulded – tested along and transverse to flow
  - Poly(butylene terephthalate) Ticona CELANEX injection moulded
- **Creep model development**
  - Application of model to above test data
- **Preparation of FE code**
  - Necessary to establish how creep data should be used in situations where the stress is not constant
  - Explore using step loading tests

# Modelling creep under tension

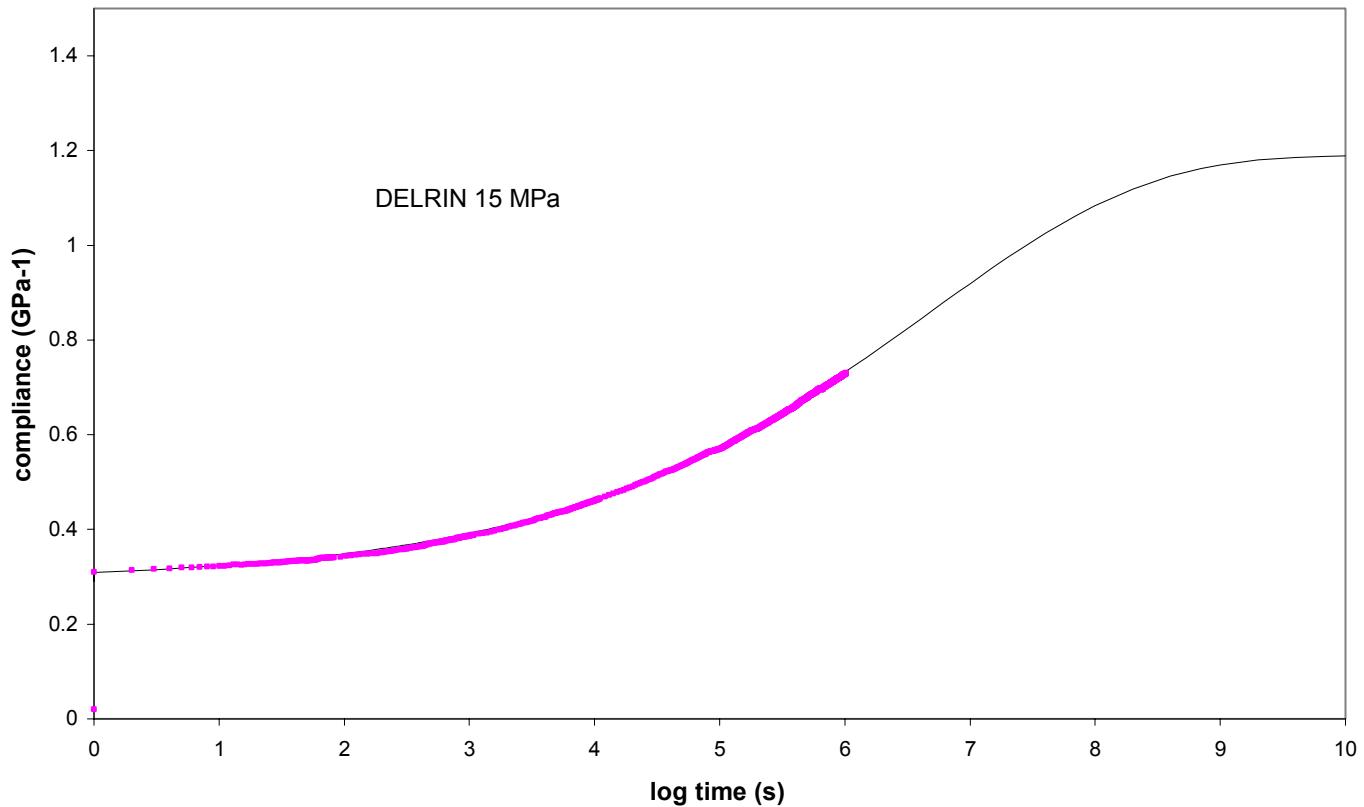
- A creep compliance function

$$D(t) = \frac{\varepsilon(t)}{\sigma_0} = D_0 + \Delta D \left( 1 - \exp - \left( \frac{t}{t_0} \right)^m \right)$$

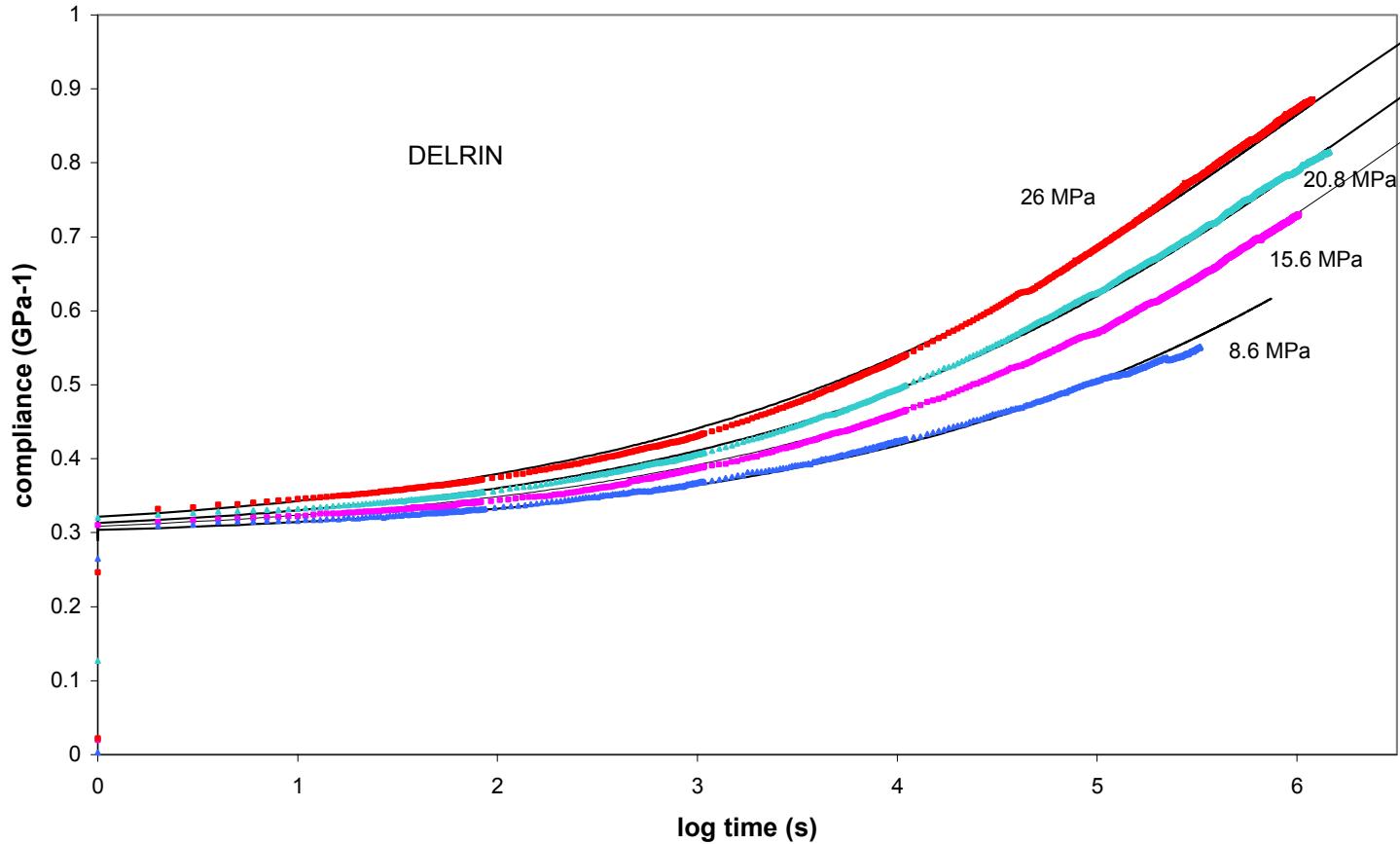
- $t_0$  is a mean retardation time



# Extrapolation to long times



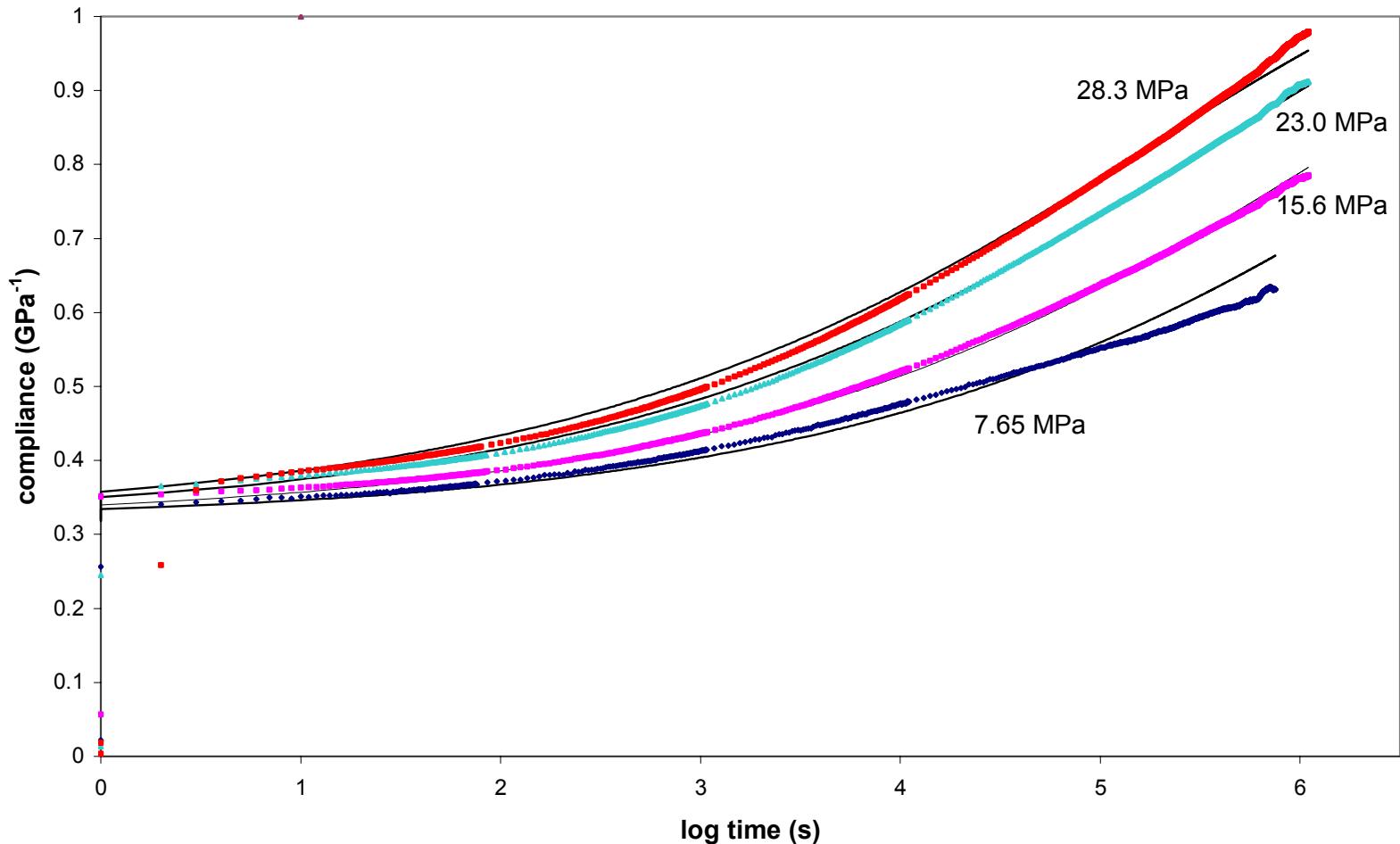
# Modelling non-linear creep DELRIN compression moulded



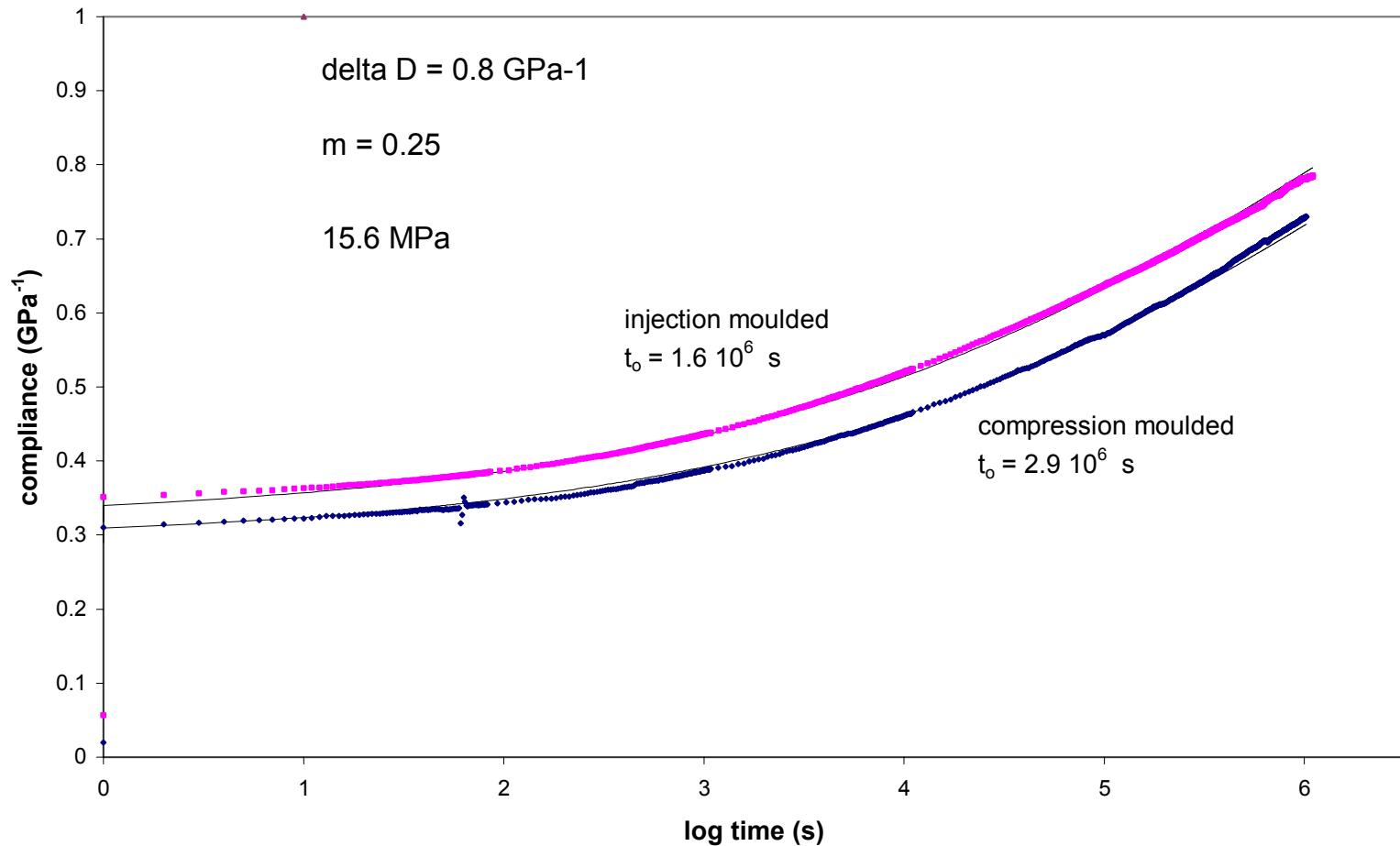
- The retardation time parameter  $t_0$  decreases with increasing stress

# OM injection moulded DELRIN

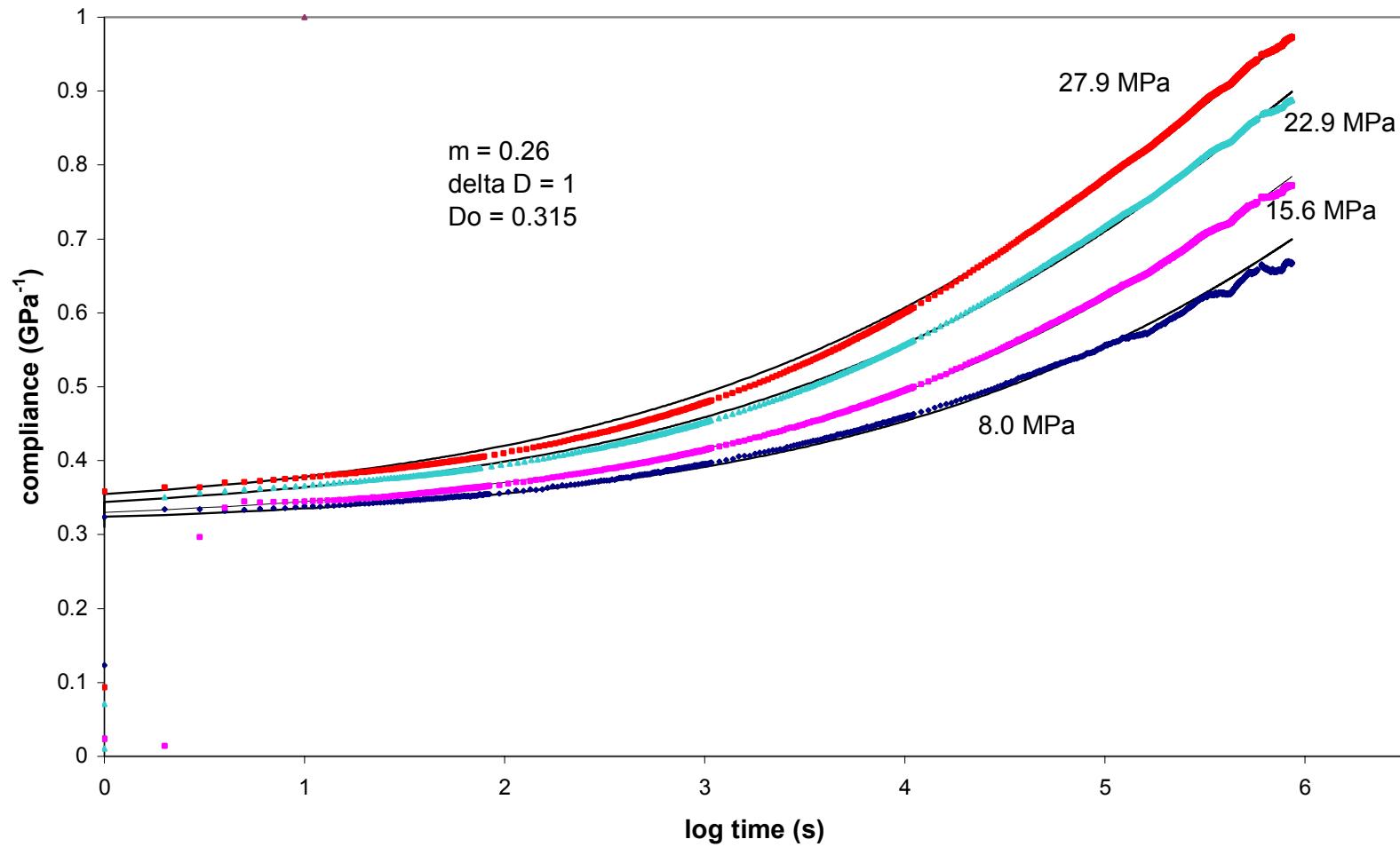
- Poor fit with constant  $m$  and  $\Delta D$



# Comparison of compression and injection moulded data - DELRIN

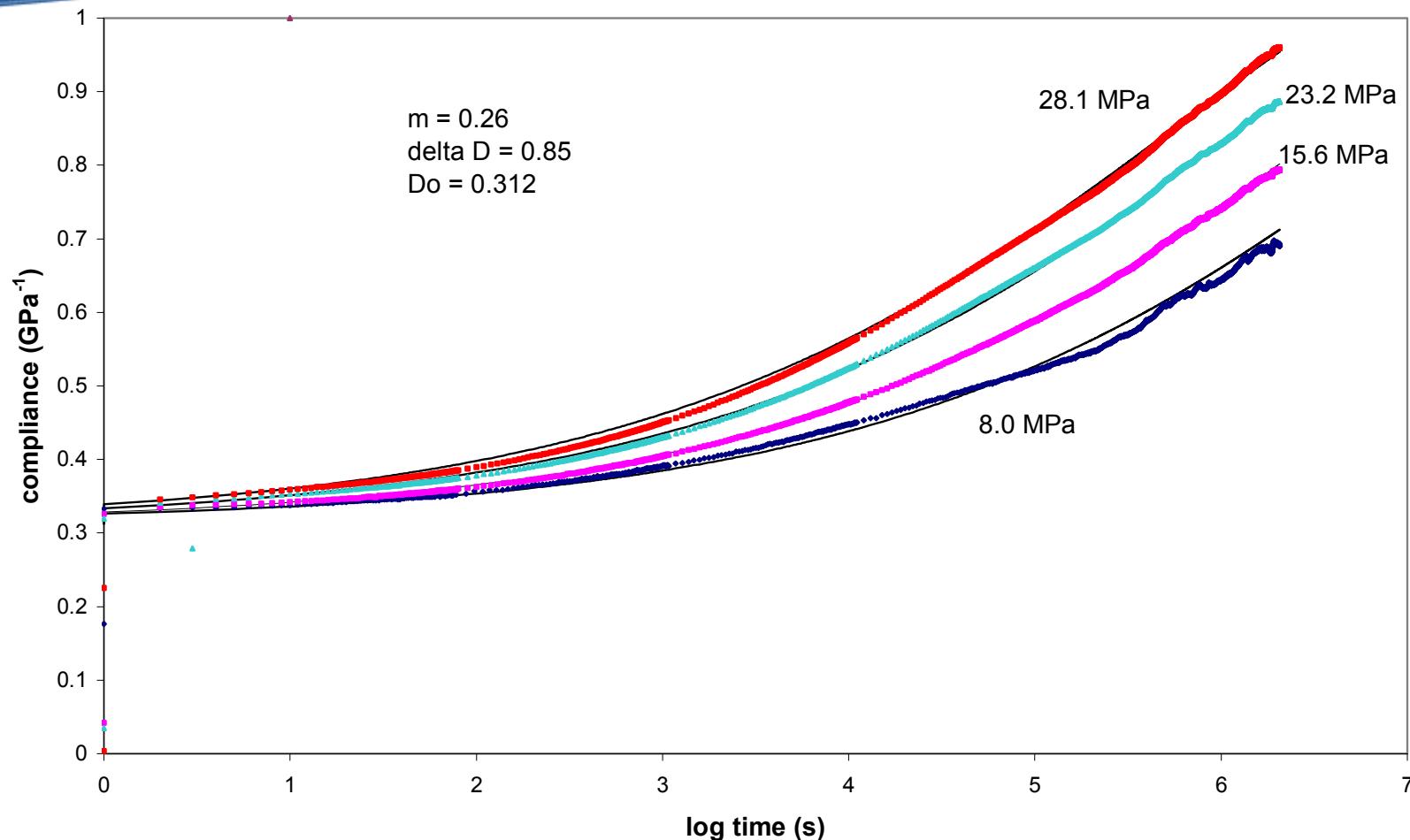


# OM injection moulded HOSTAFORM tested along flow

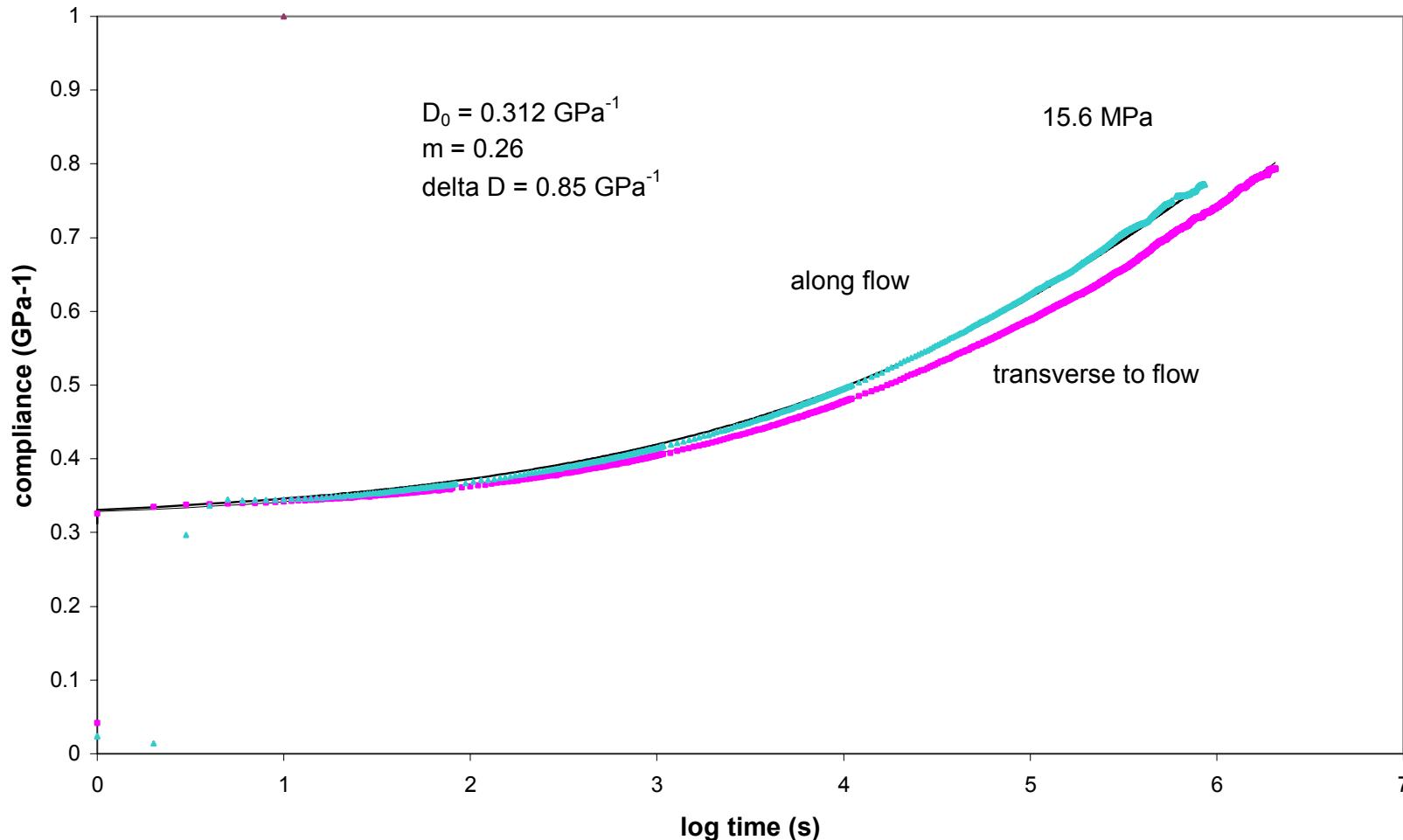


# OSTAFORM injection moulded tested transverse to flow

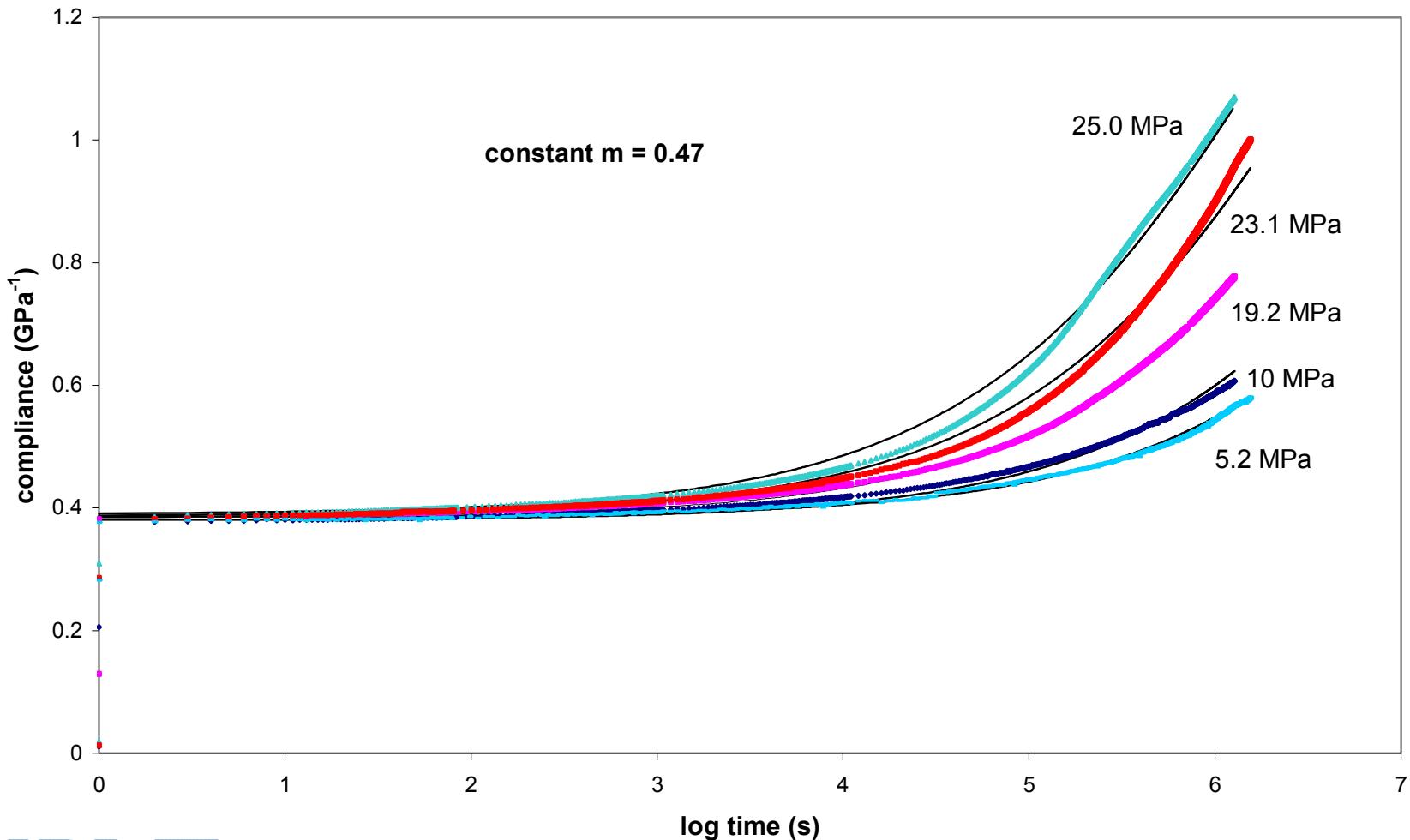
- Small reduction in  $\Delta D$



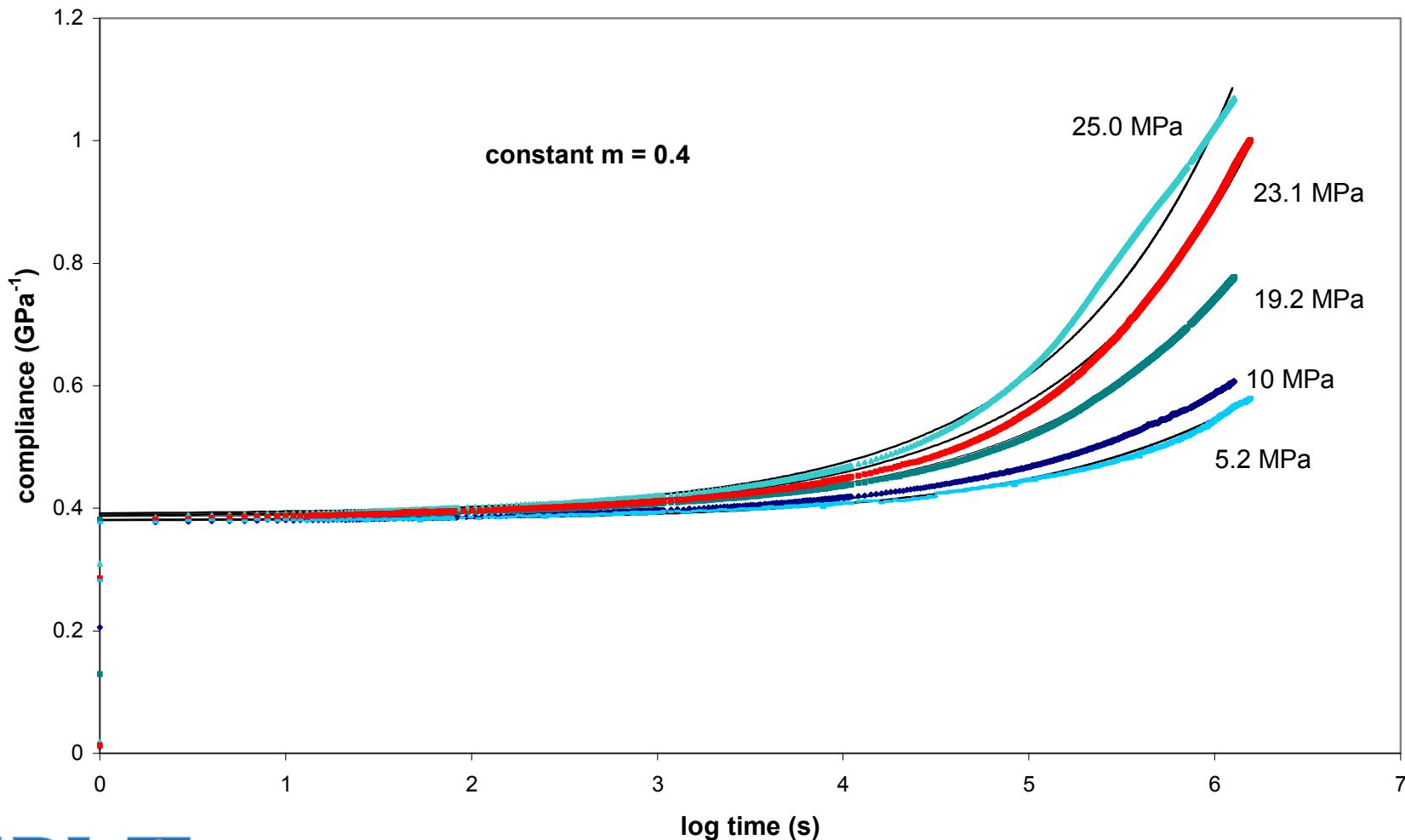
# Comparison along and transverse to flow - HOSTAFORM



# BT injection moulded CELANEX along flow



# Injection moulded CELANEX with elastic flow

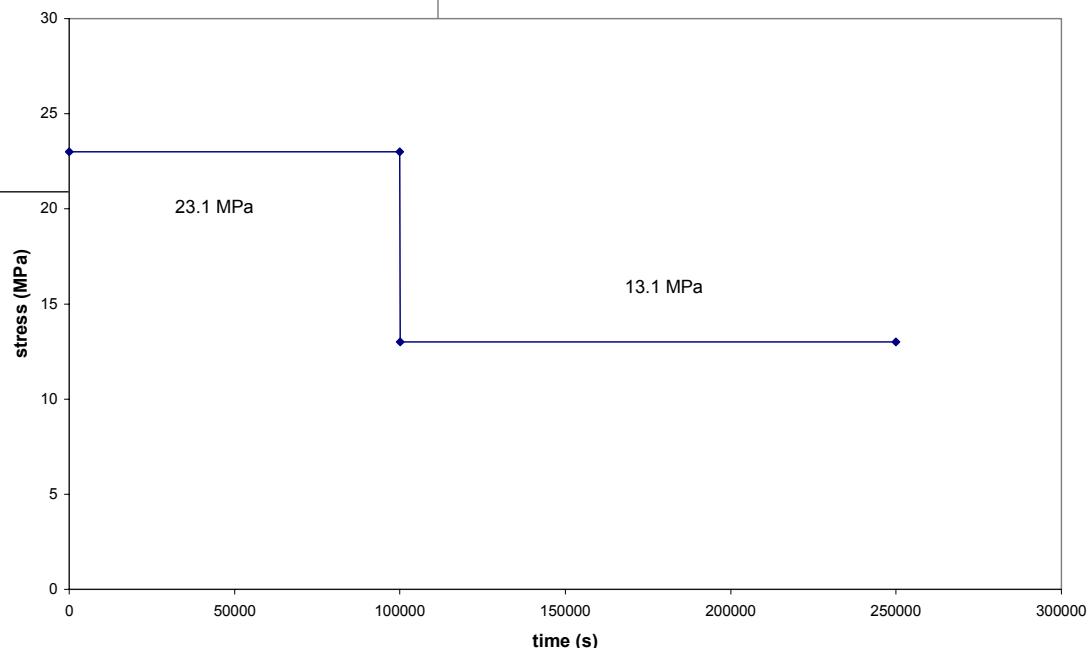
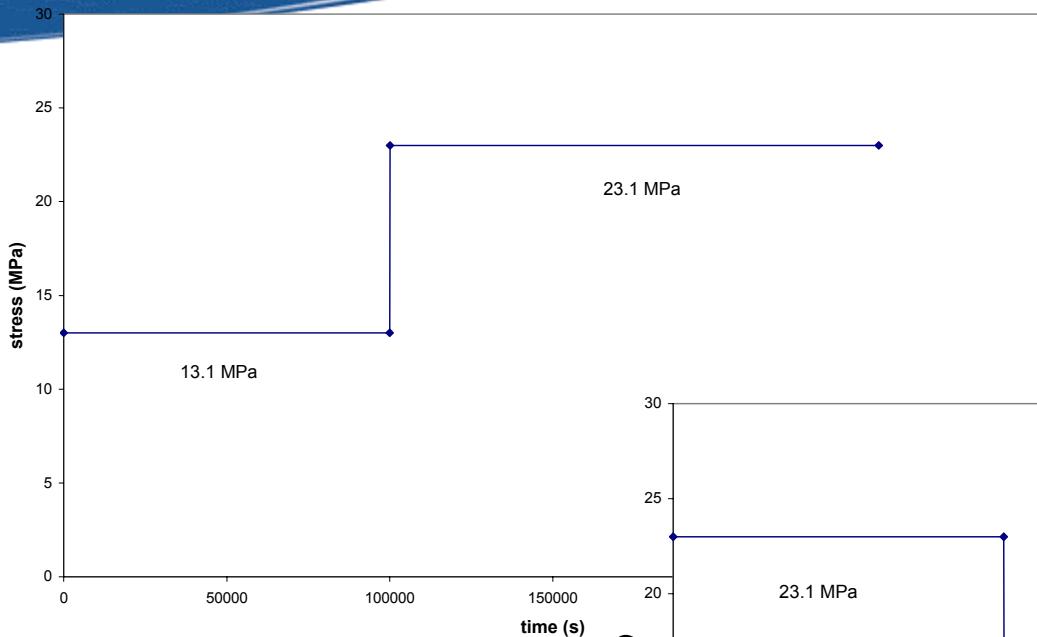


# Application of the creep model in an FE analysis

- How are creep functions to be used in situations where the stress is changing with time
- Explore using step loading tests with ABAQUS
  - Use creep functions in ABAQUS to model polymer creep

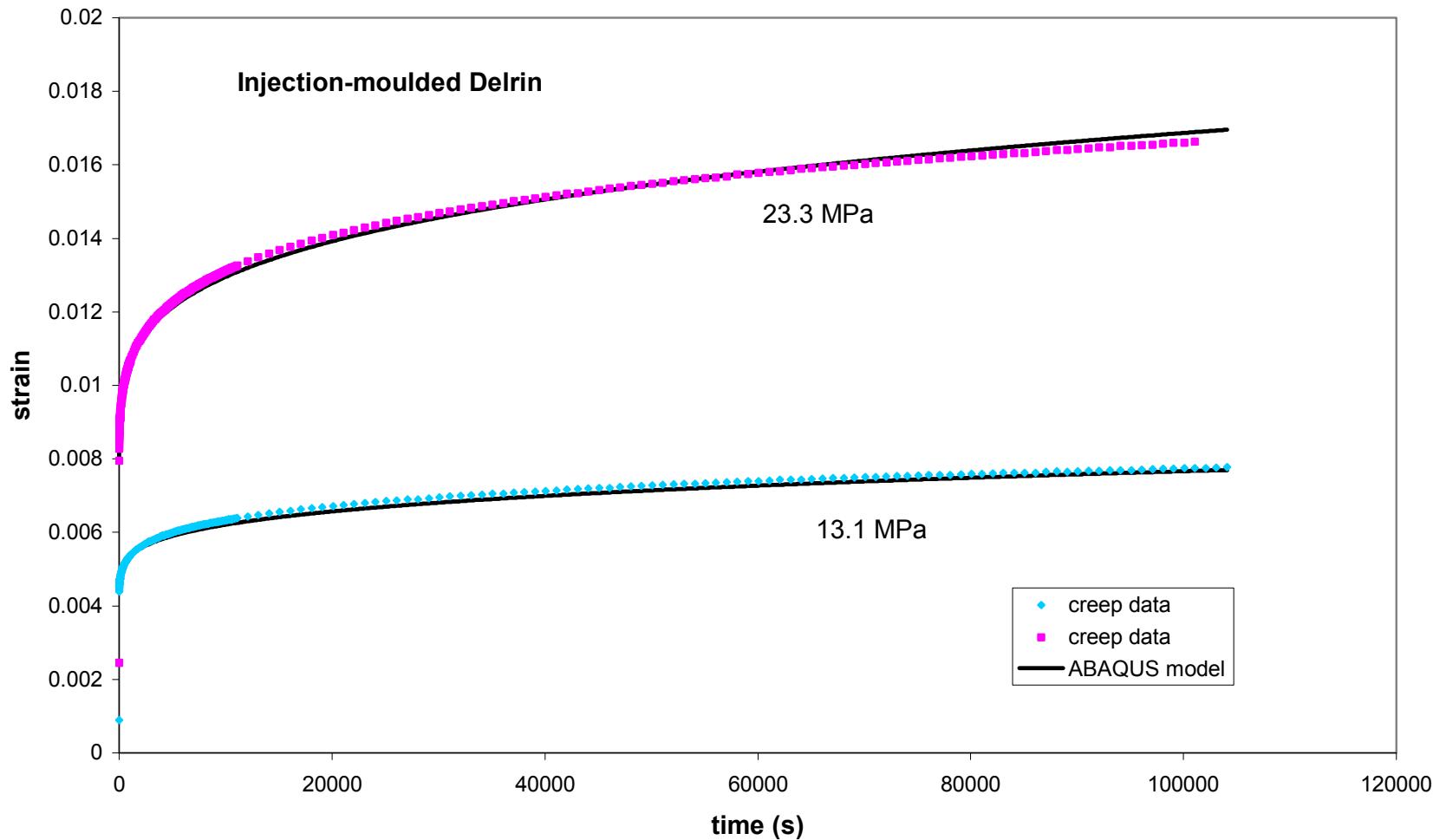
# Obtain solutions for 2-step creep tests

## Stress histories

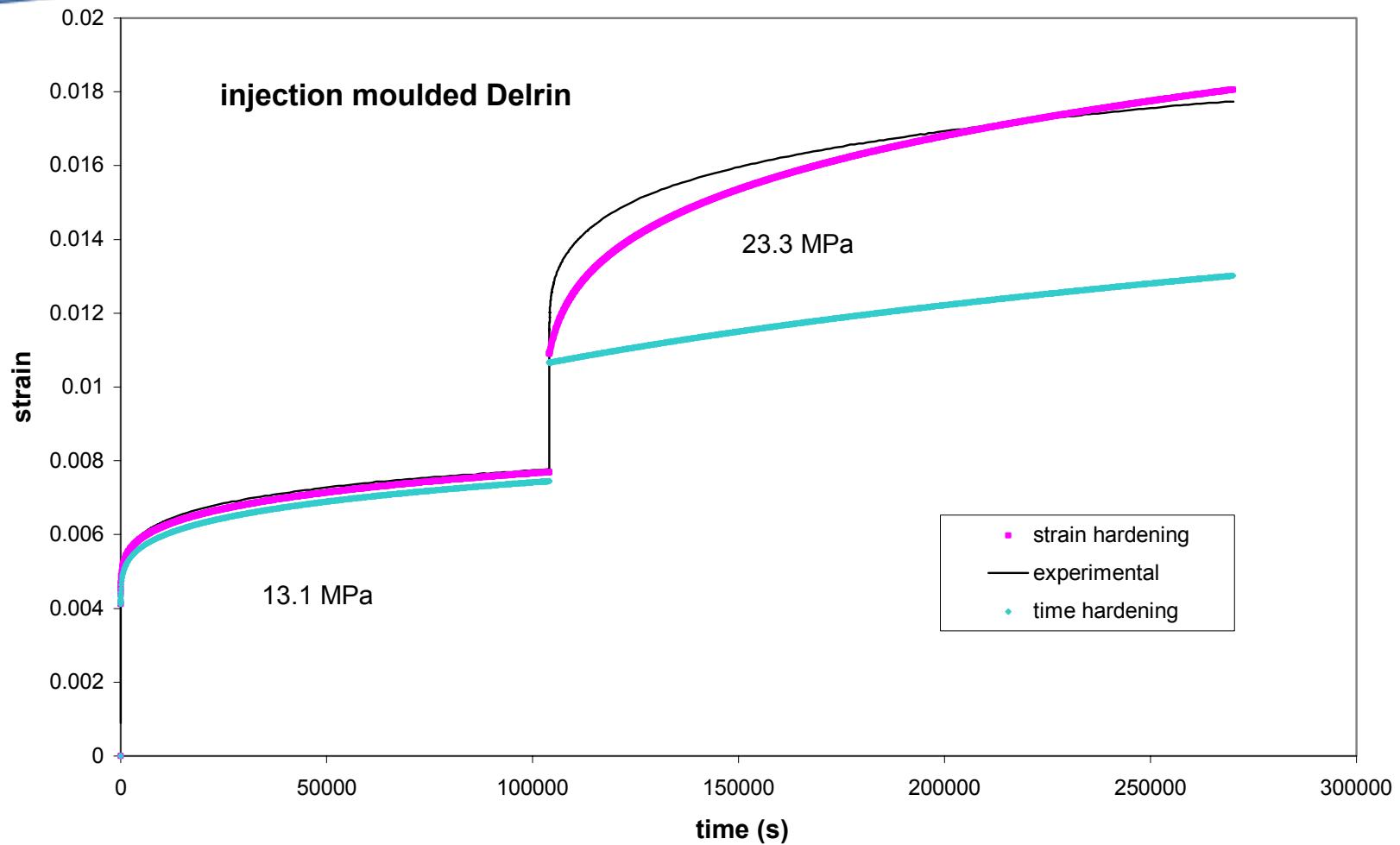


# DELIN – application of ABAQUS creep model

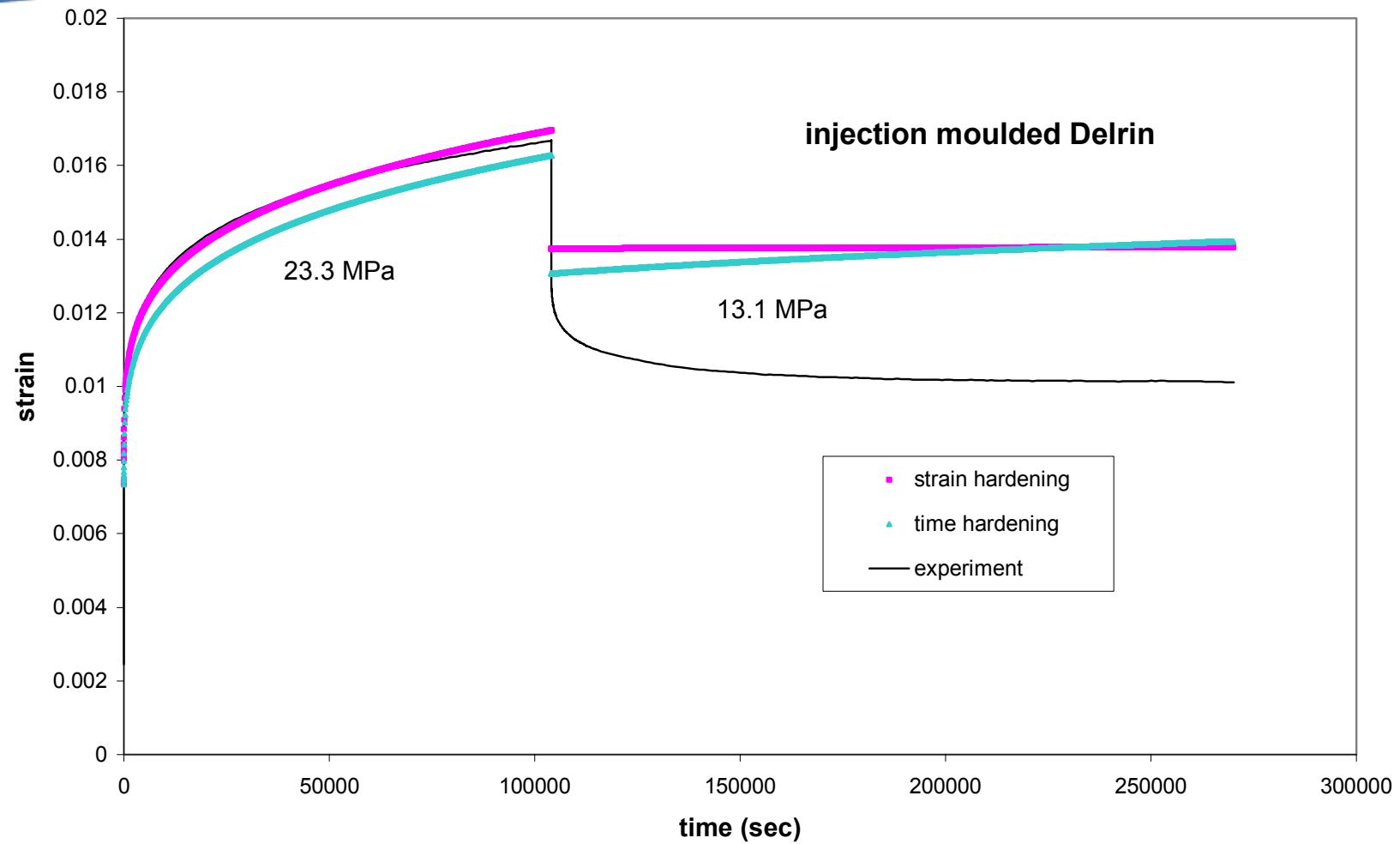
$$\varepsilon(t) = \sigma D_0 + A\sigma^n t^m$$



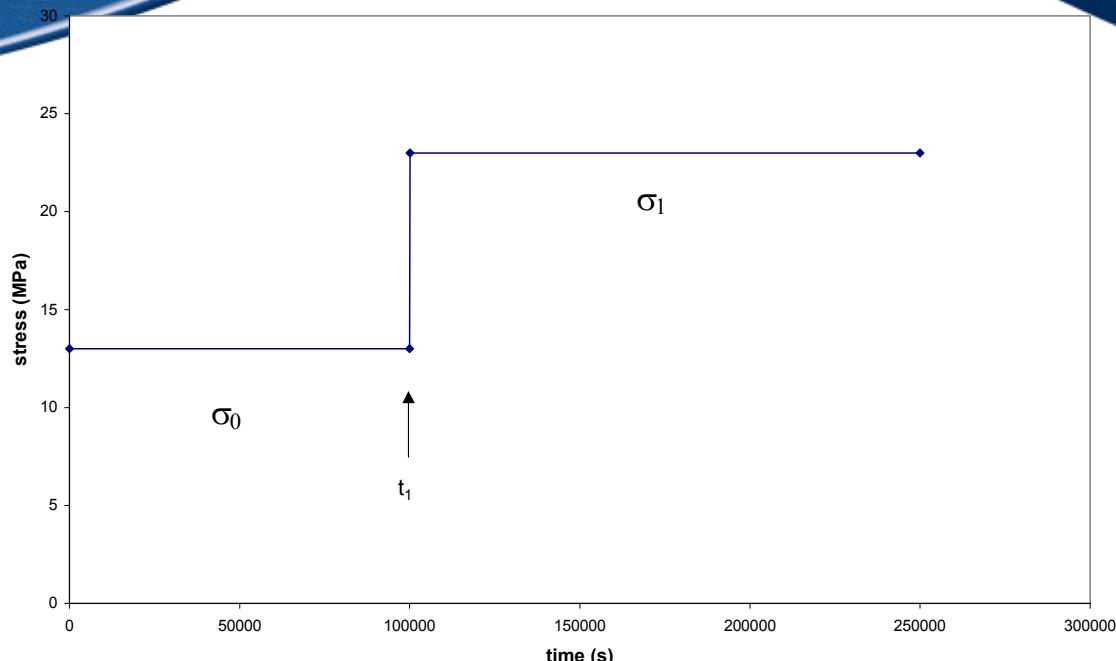
# Step loading predictions using ABAQUS



# Step unloading predictions using ABAQUS



# solution by superposition



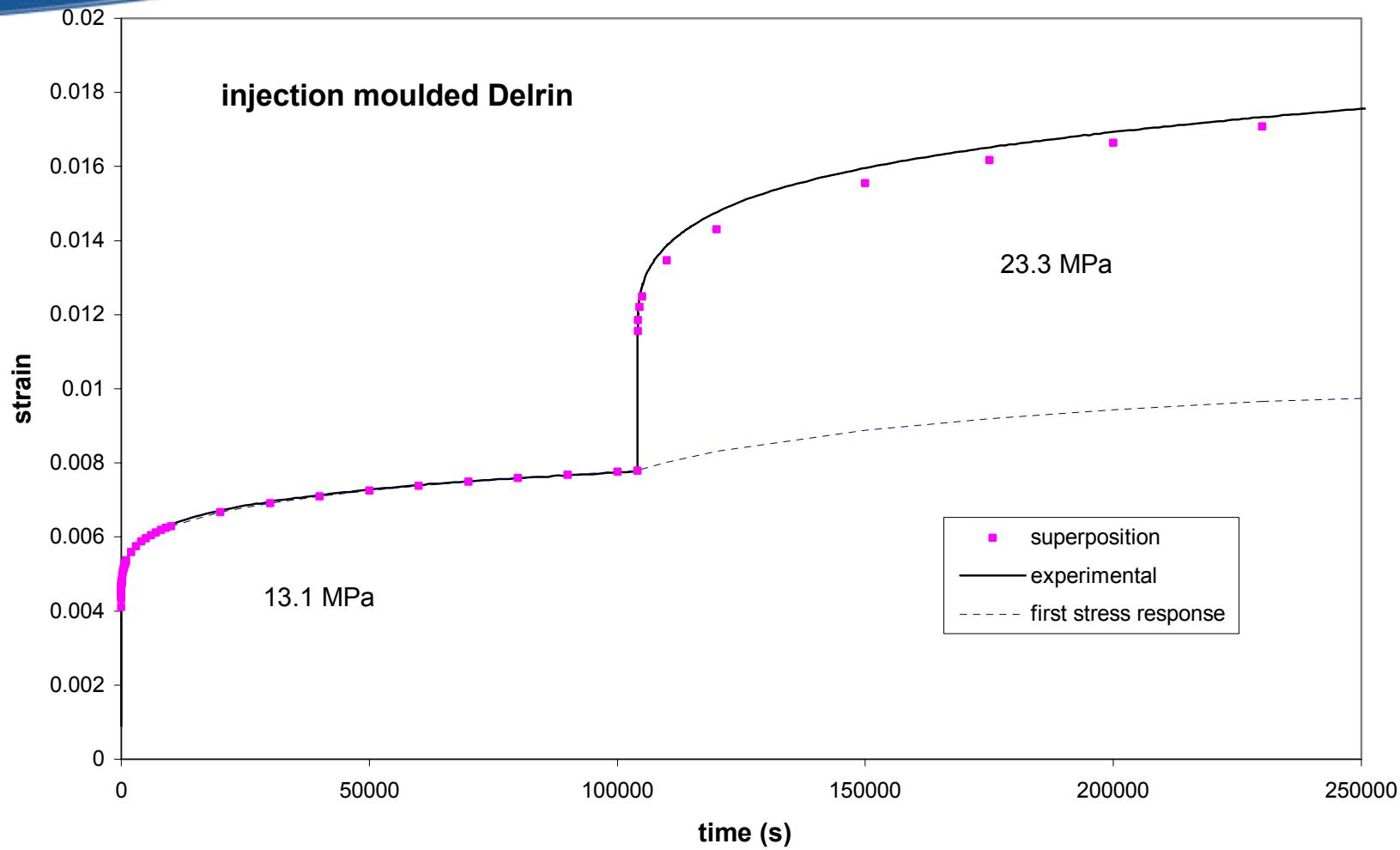
Linear behaviour

$$\varepsilon(t) = \sigma_0 D(t) + (\sigma_1 - \sigma_0) D(t - t_1)$$

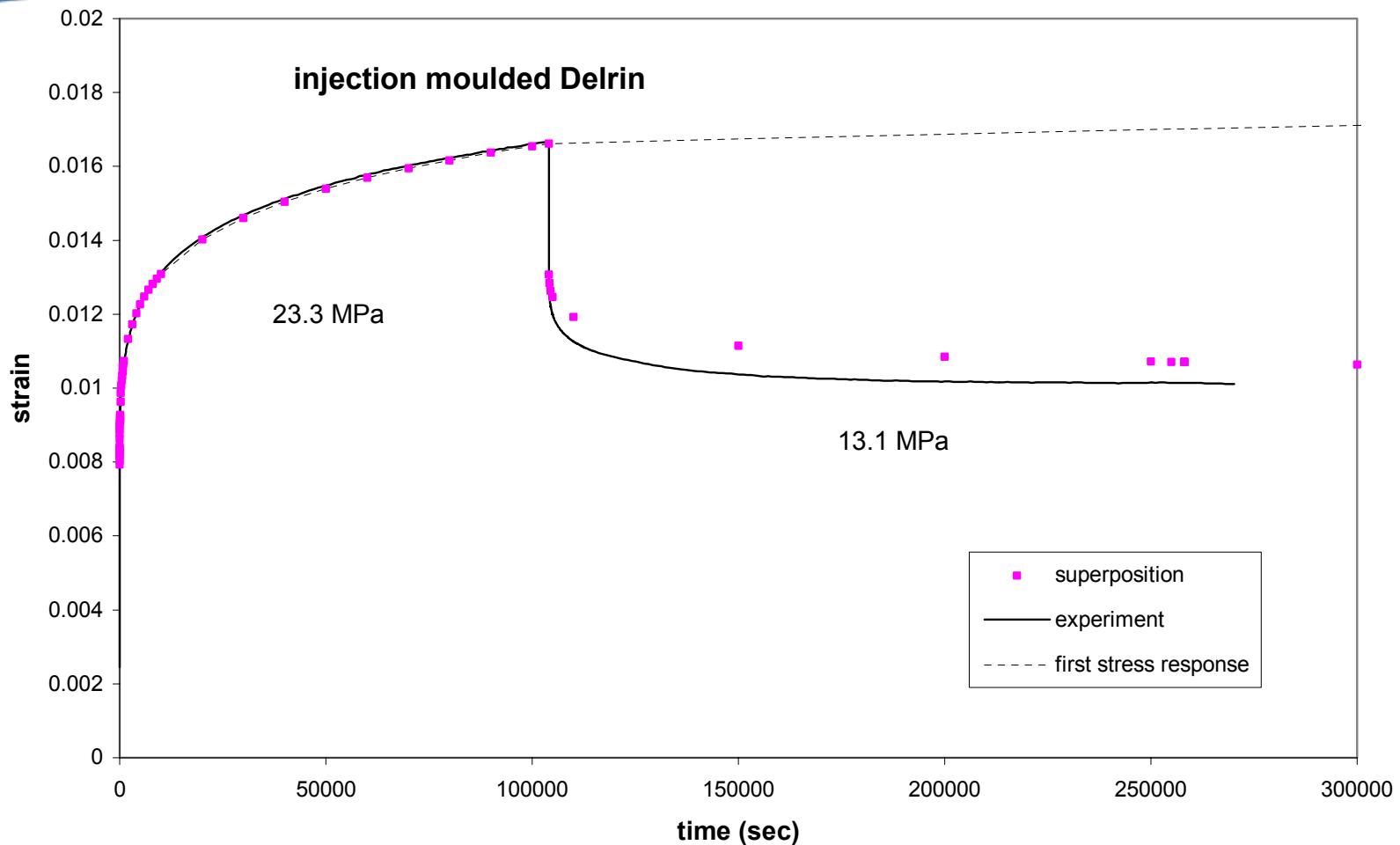
Non-linear

$$\varepsilon(t) = \sigma_0 \left[ D_0 + \Delta D \left[ 1 - \exp \left( - \left( \frac{t_1}{t_0} + \frac{t - t_1}{t_{01}} \right)^m \right) \right] \right] + (\sigma_1 - \sigma_0) \left[ D_0 + \Delta D \left[ 1 - \exp \left( - \left( \frac{t - t_1}{t_{01}} \right)^m \right) \right] \right]$$

# Comparison of superposition solution with experiment



# Comparison of superposition solution with experiment - unloading



- Generalise the superposition solution for continuous changes of stress with time.
- Use this formulation to code the model into an FE system
- Evaluate code by comparing predictions for different load histories with experiment
  - Step loading and unloading in tension
  - Creep under flexure
  - Stress relaxation
- Explore discrepancies with predictions of stress removal
- Explore modifications needed to model creep in PBT
  - Assess anisotropy in injection mouldings